# A Statistical Method for SVBRDF Approximation from Video Sequences in General Lighting Conditions (Additional Materials) 

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## Appendix A

Let $\mu, m$ and the $\sigma$ be respectively the mean, the median, and the absolute deviation of a random variable $X$. Then

$$
|\mu-m|<\sigma
$$

Proof From the Jensen's inequality we know that if $X$ is a random variable and $\varphi$ is a convex function, then $\varphi(\mathbb{E}[X]) \leq$ $\mathbb{E}[\varphi(X)]$. Then we have

$$
\begin{aligned}
|\mu-m| & =|\mathbb{E}[X]-m| \\
& =|\mathbb{E}[X-m]| \\
& \leq \mathbb{E}[|X-m|] \\
& \leq \mathbb{E}[|X-\mu|]=\sigma
\end{aligned}
$$

where the first inequality comes from the Jensen's inequality applied to the absolute value function, which is convex. The second inequality is true because the median minimizes the absolute deviation.

## Appendix B

Given the unknown $\rho_{s}$ and $\alpha$ the following system of equations:

$$
\left\{\begin{array}{l}
\rho_{s} A^{\alpha}=L_{A}-L_{d}  \tag{1}\\
\rho_{s} B^{\alpha}=L_{B}-L_{d}
\end{array}\right.
$$

can be solved by applying the logarithm to both the equations:

$$
\left\{\begin{array}{l}
\alpha=\frac{\left(\ln \left(L_{A}-L_{d}\right)-\ln \left(\rho_{s}\right)\right)}{\ln (A)}  \tag{2}\\
\alpha=\frac{\left(\ln \left(L_{B}-L_{d}\right)-\ln \left(\rho_{s}\right)\right)}{\ln (B)}
\end{array}\right.
$$

and by setting the equality between the two equations:

$$
\begin{equation*}
\frac{\left(\ln \left(L_{A}-L_{d}\right)-\ln \left(\rho_{s}\right)\right)}{\ln (A)}=\frac{\left(\ln \left(L_{B}-L_{d}\right)-\ln \left(\rho_{s}\right)\right)}{\ln (B)} \tag{3}
\end{equation*}
$$

From equation 3 we compute the value:

$$
\begin{equation*}
\rho_{s}=e^{C} \tag{4}
\end{equation*}
$$

where:

$$
\begin{equation*}
C=\frac{\ln \left(L_{B}-L_{d}\right) \ln (A)-\ln \left(L_{A}-L_{d}\right) \ln (B)}{\ln (A)-\ln (B)} \tag{5}
\end{equation*}
$$

With the value of $\rho_{s}$ we recover the value of $\alpha$ by solving one of the equation in the system 2 .
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Figure 1: Camera path reconstructed with the registration algorithm: (Top-Left) HEAD; (Top-Right) SLEEPING BUDDHA; (Bottom-Left) DWARF; (Bottom-Right) GNOME.


Figure 2: Quality computation: (Left) map of the border distance from the depth discontinuities; (Left-Center) depth map; (Right-Center) dot product between the normal and the view direction; (Right) final quality.
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Figure 3: Comparison of environment maps: (Top-Left) first real environment scenario; (Top-Center) first environment scenario reconstructed from the DWARF's videos; (Top-Right) first environment scenario reconstructed from the GNOME's videos;(Bottom-Left) second real environment scenario; (Bottom-Center) second environment scenario reconstructed from the HEAD's videos; (Bottom-Right) second environment scenario reconstructed from the SLEEPING BUDDHA's videos.
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Figure 4: Segmentation of the basis materials: (Top-Left) HEAD; (Top-Right) SLEEPING BUDDHA; (Bottom-Left) DWARF; (Bottom-Right) GNOME. For each image there is the rendering of the object with the diffuse color (left) and the rendering in false color of the basis materials (right).
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Figure 5: HEAD: (Left) rendering; (Right) original frame.
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Figure 6: SLEEPING BUDDHA: (Left) rendering; (Right) original frame.


Figure 7: DWARF: (Left) rendering; (Right) original frame.


Figure 8: GNOME: (Left) rendering; (Right) original frame.
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Figure 9: Rendering of the SLEEPING BUDDHA with the "Uffizi Gallery" environment map
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Figure 10: Rendering of the SLEEPING BUDDHA with the "Dining room" environment map
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Figure 11: Rendering of the SLEEPING BUDDHA with the "Pisa" environment map

